

## 第八次作业 (Flatten Real-Analytic Boundary)

请于四月二十五日周五 (校历第十周) 当堂上交本次作业。请独立完成。如有参与讨论者, 请引用或致谢他们。

1. Let  $\gamma$  be a regular real-analytic curve in  $\mathbb{C}$ . More precisely,  $\gamma(t) = (x(t), y(t)) \in \mathbb{C}$  for  $t \in (-1, 1)$  such that  $x(t), y(t)$  are real-analytic in  $t$  and  $x'(t), y'(t) \neq 0$  for any  $t \in (-1, 1)$ . Prove that there is an open neighborhood  $\Omega$  of  $\gamma(0)$  in  $\mathbb{C}$  and a biholomorphic map  $f : \Omega \rightarrow \Omega' \subset \mathbb{C}$  such that  $f(\gamma(t))$  is mapped into a line in  $\Omega' \subset \mathbb{C}$ .