

## 第三次作业

请于四月五日周五 (校历第七周) 当堂上交本次作业。只收纸质版。晚交不收。可以与班上同学讨论合作, 请参与合作的同学共同交一份作业, 并署上所有参与者姓名。

1. Let  $f \neq 0$  be a holomorphic function on the disc  $B_r(0)$  in  $\mathbb{C}$ . Let  $h_a$  be a holomorphic function on  $B_r(0)$ , which satisfies  $h_a(0) = 0$  and  $h_a(b) = 1$  for any  $b^k = a$  ( $k$  is a positive integer), where  $a \in B_r(0)$  whose norm is small enough. Then we have

$$\int_{B_r(0)} |f|^2 |h_a|^2 > C_1 |a|^{-2}, \quad (1)$$

where  $C_1$  is a positive constant independent of  $a$  and  $h_a$ .